GCSE

wjec cbac

3310U60-1

Z22-3310U60-1

TUESDAY, 7 JUNE 2022 – MORNING

MATHEMATICS – NUMERACY
UNIT 2: CALCULATOR-ALLOWED
HIGHER TIER

1 hour 35 minutes

ADDITIONAL MATERIALS

A calculator will be required for this paper.

A ruler, a protractor and a pair of compasses may be required.

INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.

You may use a pencil for graphs and diagrams only.

Write your name, centre number and candidate number in the spaces at the top of this page.

Answer **all** the questions in the spaces provided.

If you run out of space, use the additional page at the back of the booklet. Question numbers must be given for the work written on the additional page.

Take π as 3·14 or use the π button on your calculator.

INFORMATION FOR CANDIDATES

You should give details of your method of solution when appropriate.

Unless stated, diagrams are not drawn to scale.

Scale drawing solutions will not be acceptable where you are asked to calculate.

The number of marks is given in brackets at the end of each question or part-question.

In question **3**, the assessment will take into account the quality of your linguistic and mathematical organisation, communication and accuracy in writing.

For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1.	10	
2.	12	
3.	7	
4.	4	
5.	4	
6.	6	
7.	7	
8.	4	
9.	5	
10.	11	
Total	70	

Formula List – Higher Tier

Area of trapezium $= \frac{1}{2}(a + b)h$
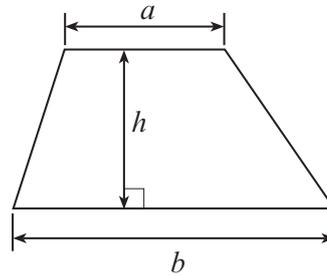
Volume of prism = area of cross-section × length
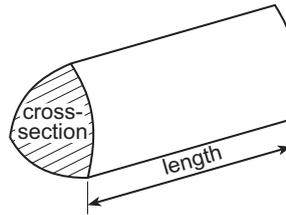
Volume of sphere $= \frac{4}{3}\pi r^3$

Surface area of sphere $= 4\pi r^2$
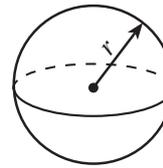
Volume of cone $= \frac{1}{3}\pi r^2 h$

Curved surface area of cone $= \pi r l$
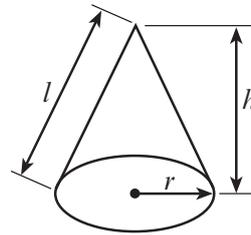
In any triangle ABC

    Sine rule $\dfrac{a}{\sin A} = \dfrac{b}{\sin B} = \dfrac{c}{\sin C}$

    Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$

    Area of triangle $= \frac{1}{2}ab \sin C$
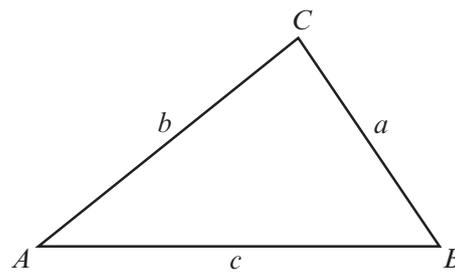
The Quadratic Equation

The solutions of $ax^2 + bx + c = 0$ where $a \neq 0$ are given by $x = \dfrac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$

Annual Equivalent Rate (AER)

AER, as a decimal, is calculated using the formula $\left(1 + \dfrac{i}{n}\right)^n - 1$, where i is the nominal interest rate per annum as a decimal and n is the number of compounding periods per annum.

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Turn over.

1. (a) Last year, Janita recorded the number of miles she travelled each week in her car. She summarised the information in a frequency table, as shown below.

Number of miles, x	Frequency
$20 \leqslant x < 60$	4
$60 \leqslant x < 80$	8
$80 \leqslant x < 100$	11
$100 \leqslant x < 150$	12
$150 \leqslant x < 200$	17

(i) In which group does the median weekly number of miles lie?
Circle your answer. [1]

$20 \leqslant x < 60$ $80 \leqslant x < 100$ $150 \leqslant x < 200$

$60 \leqslant x < 80$ $100 \leqslant x < 150$

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(ii) Calculate an estimate of the mean number of miles Janita travelled each week in her car. [4]

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(b)   Last month:
  •   Janita travelled 440 miles in her car
  •   the cost of fuel was £1.30 per litre.

Janita's car averages 11 miles per litre of fuel.

Next month, she needs to budget for an increased travel cost.

Janita says,

> The number of miles I travel will increase by 12%.
> The cost of fuel will increase by 10% next month.

Calculate how much Janita should budget for her car travel costs for next month.
You must show all your working. [5]

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Turn over.

2. Mito is a city in Japan.
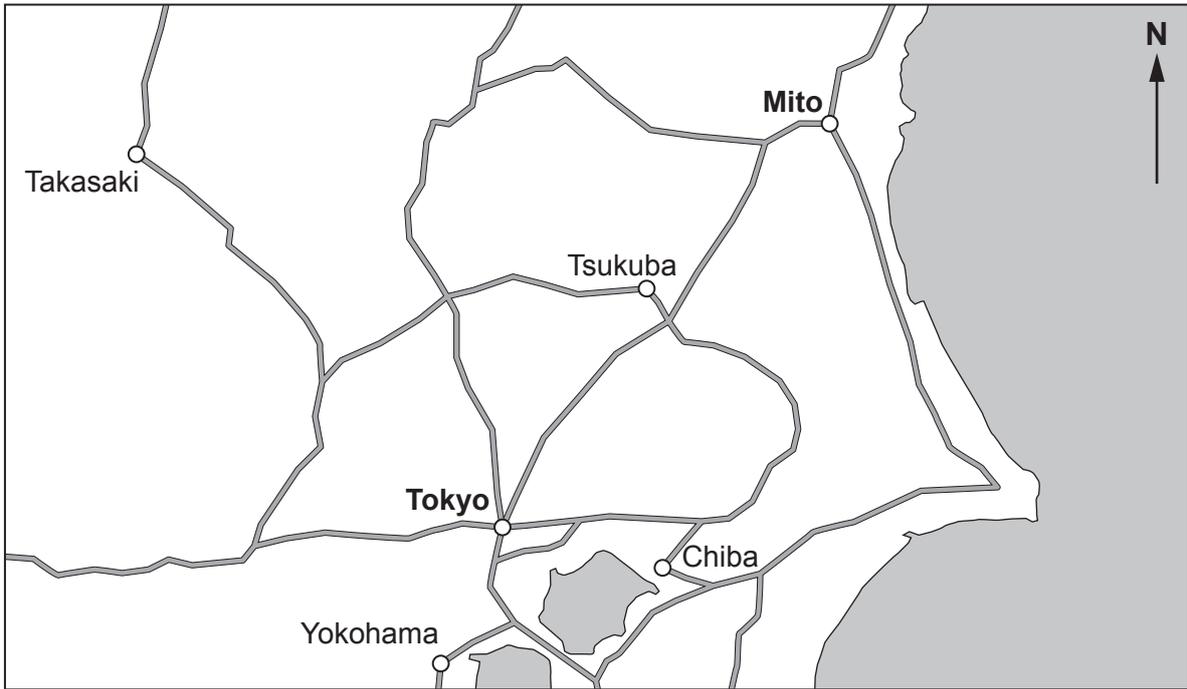
(a) The road distance from Mito to Tokyo is 114 km.
Anzu travelled by car from Mito to Tokyo in 1 hour 27 minutes.

Calculate the average speed of Anzu's journey.
Give your answer in km/h. [3]

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(b)   Tilly is travelling to Mito.
She wants to exchange no more than £800 into Japanese yen.

The exchange rate is £1 = 135.72 Japanese yen.

On the day Tilly exchanges her money, the exchange shop only has 1000 Japanese yen notes and 5000 Japanese yen notes available.

Calculate:
  •   the maximum number of Japanese yen Tilly can buy
  •   how much, to the nearest penny, this will cost her.

You must show all your working.   [5]

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(c)   Mito has a population of 270 400.

25% of Mito's population is aged 65 or over.
The ratio of the number of people aged 0 to 14 to the number of people aged 15 to 64 is 9 : 41.

Calculate the number of people aged 0 to 14.   [4]

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Turn over.

3. *In this question, you will be assessed on the quality of your organisation, communication and accuracy in writing.*

A motorcyclist leans into a corner on a motorcycle.
The angle of lean is the angle between the vertical and the motorcycle.

When the motorcycle is upright, the centre of the handlebars is 110 cm above the ground.
The diagrams below illustrate a front view of a motorbike as its rider goes into a corner.

The motorcycle is vertical to begin with. It then leans 30 cm horizontally into the corner.
The motorcycle then leans a further 30 cm into the corner, with a total horizontal lean distance of 60 cm.

**Diagrams not
drawn to scale**

30 cm

110 cm

Angle
of lean

110 cm

60 cm

Angle
of lean

110 cm

Before the corner   Lean of 30 cm into the corner   Lean of 60 cm into the corner

Show that the angle of lean more than doubles as the motorcycle leans from 30 cm horizontally to 60 cm horizontally.
Your must show all your working.

[5 + 2 OCW]

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4. A cylindrical water tank has a radius of 36 cm.
There are 80 litres of water in the tank.

Calculate the height of the water in the tank in centimetres. [4]

Diagram not drawn to scale

Height of water

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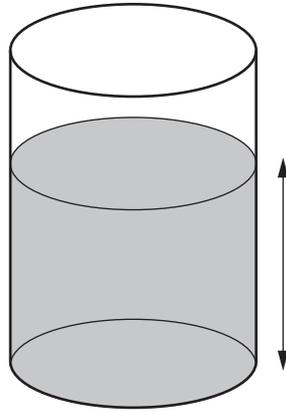
The height of the water in the tank is .... cm

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5. Last year, Khalida paid 2400 dollars income tax.
The tax bands were as follows.

Band	Taxable income	Tax rate
Personal allowance	Up to 5000 dollars	0%
Basic rate	5000 dollars to 25 000 dollars	20%

Calculate Khalida's income before the deduction of tax. [4]

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Khalida's income was .... dollars

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Turn over.

6. Dewi and Cai are building a fence.
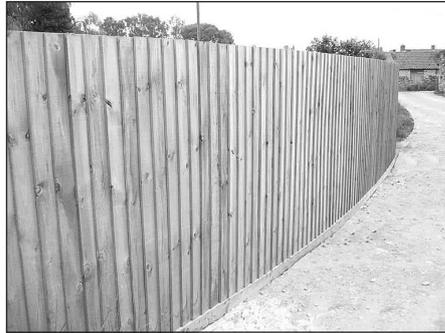
They are using fence boards that overlap each other.
The diagrams below show the first 3 boards in position, and how the boards overlap.

Fence boards
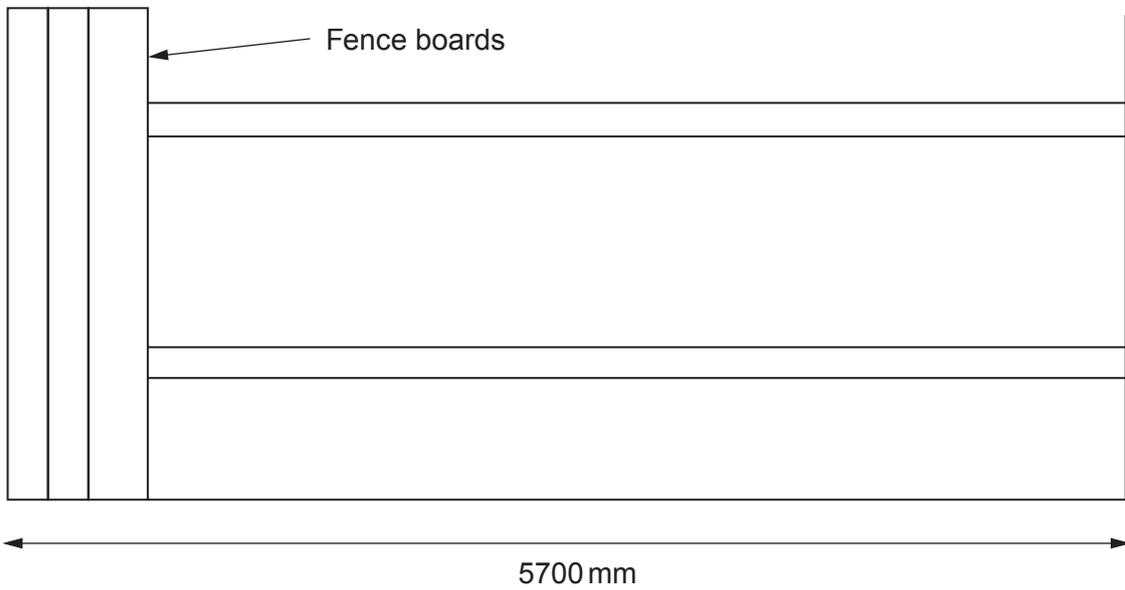
5700 mm

Plan view of how the boards overlap

20 mm   100 mm
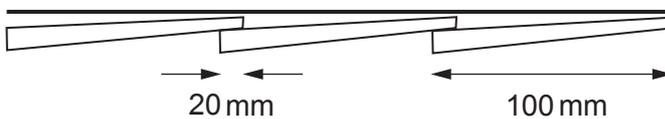
Diagrams not drawn to scale

The fence needs to cover a length of 5700 mm, correct to the nearest 100 mm.
When in position, each board has a width of 100 mm, correct to the nearest 5 mm.
Each overlap is **exactly** 20 mm, as shown in the diagram above.

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Calculate the minimum number of boards that Dewi and Cai need to buy to guarantee that they have enough to build the fence.
You must show all your working. [6]

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7. Tubu is a company that makes chocolate bars.
The packaging for a new chocolate bar is in the shape of an isosceles triangular prism.

To open the packaging, Tubu is considering adding a tear strip.

The tear strip will go from *A* to *B*, *B* to *C*, and then from *C* back to *A*.

Some of the dimensions of the packaging are shown in the diagram below.
DB = *DC*.

Diagram not drawn to scale

Calculate the **total** length of the tear strip required for the packaging. [7]

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8. On 1st January 2022, Jay invested £850 in the Savrplus savings account with 'Banc y Ddraig'. The Savrplus account pays interest at a rate of 0·48% every month. The interest is paid on the last day of every month.
Jay does not plan to withdraw any money or make any further payments into the account.

Calculate the date when Jay will first have over £1000 in his account. [4]

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Date when Jay will first have over £1000 in his account is ....

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9. SureCan is a company that makes cylindrical cans for the food industry.
Two of the cans it makes are mathematically similar.
They are shown below.

Diagrams not drawn to scale

height

12 cm

The base area of the large can is 2·25 times the base area of the small can.

(a)   Show that the height of the small can is 8 cm.   [3]

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(b)   The volume of the small can is 144 cm^3.
Calculate the base area of the large can.   [2]

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10. Rhian is playing golf.
The diagram below shows one of the holes she is playing.
The dotted lines show the recommended route to the hole, taking 2 shots.
The length of a shot is the straight-line distance as measured on horizontal ground.

The recommended first shot is 160 yards. This shot is to a point equidistant from the sand and the tree on the corner. It is then followed by a second shot of 148 yards to the hole.

148 yds

Hole

Sand

Diagram not drawn to scale

160 yds
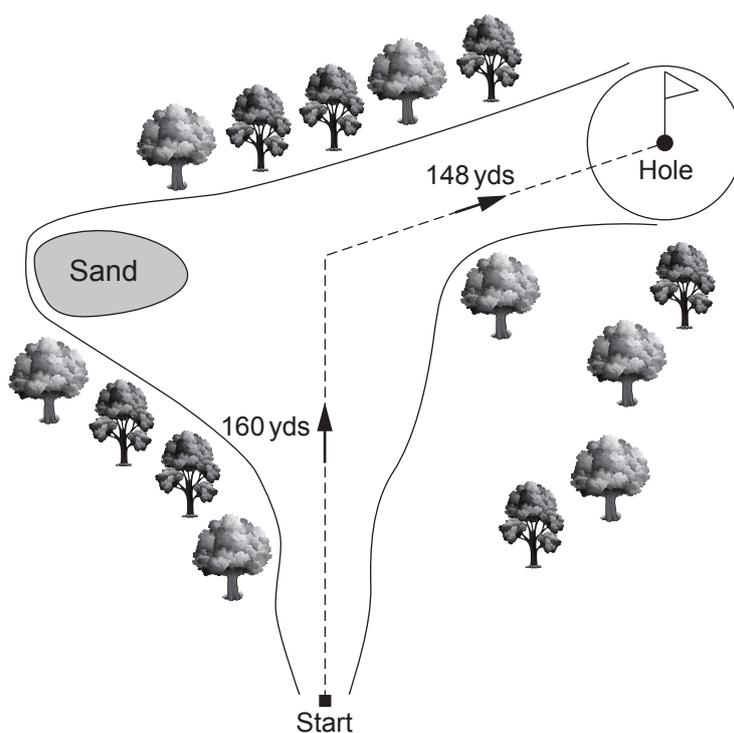
Start

(a) Rhian's map of the golf course shows her the following information about the first shot.

65 yds

Sand

160 yds

160 yds

x x

Diagram not drawn to scale

Start

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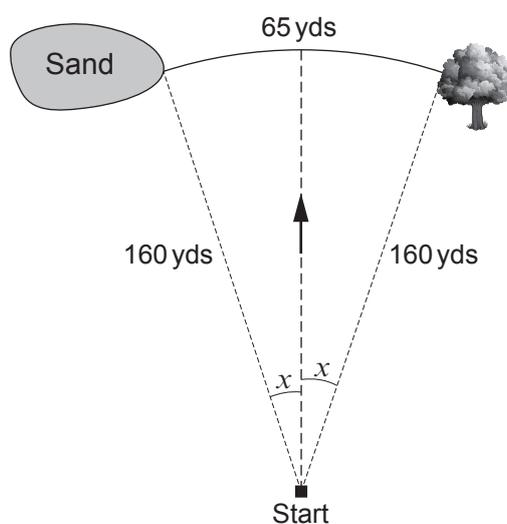
It shows an arc of a circle of length 65 yards, with its centre at the start.
Rhian does not want her first shot to land in the trees or in the sand.
The greatest angle she can hit her first shot to the right or left of the recommended line
has been shown on the diagram as x.

Calculate the size of angle x, giving your answer correct to 3 significant figures.　　　[4]

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TURN OVER

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(b) Rhian is considering hitting a single shot over the trees and straight at the hole.
To get over the trees, this shot needs to be longer than 160 yards.

148 yds

Hole

Sand

Diagram not drawn to scale

160 yds

Single shot

32°

Start

Calculate the length of this single shot.   [7]

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END OF PAPER

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Question number	Additional page, if required. Write the question number(s) in the left-hand margin.

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