

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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**Pearson Edexcel Level 3 GCE**

**Thursday 25 May 2023**

Afternoon  
(Time: 1 hour 30 minutes)

Paper  
reference

**9FM0/01**

**Further Mathematics**

**Advanced**

**PAPER 1: Core Pure Mathematics 1**

**You must have:**

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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3.

**In this question you must show all stages of your working.****Solutions relying on calculator technology are not acceptable.**

$$z_1 = -4 + 4i$$

- (a) Express  $z_1$  in the form  $r(\cos \theta + i \sin \theta)$ , where  $r \in \mathbb{R}$ ,  $r > 0$  and  $0 \leq \theta < 2\pi$  (2)

$$z_2 = 3 \left( \cos \frac{17\pi}{12} + i \sin \frac{17\pi}{12} \right)$$

- (b) Determine in the form  $a + ib$ , where  $a$  and  $b$  are exact real numbers,

(i)  $\frac{z_1}{z_2}$  (2)

(ii)  $(z_2)^4$  (2)

- (c) Show on a single Argand diagram

(i) the complex numbers  $z_1$ ,  $z_2$  and  $\frac{z_1}{z_2}$

(ii) the region defined by  $\{z \in \mathbb{C} : |z - z_1| < |z - z_2|\}$  (4)











4. Prove by induction that for  $n \in \mathbb{N}$

$$\begin{pmatrix} 1 & -2 \\ 0 & 1 \end{pmatrix}^n = \begin{pmatrix} 1 & -2n \\ 0 & 1 \end{pmatrix}$$

(5)

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8. A colony of small mammals is being studied.  
In the study, the mammals are divided into 3 categories

$N$ (newborns)	0 to less than 1 month old
$J$ (juveniles)	1 to 3 months old
$B$ (breeders)	over 3 months old

- (a) State one limitation of the model regarding the division into these categories. (1)

A model for the population of the colony is given by the matrix equation

$$\begin{pmatrix} N_{n+1} \\ J_{n+1} \\ B_{n+1} \end{pmatrix} = \begin{pmatrix} 0 & 0 & 2 \\ a & b & 0 \\ 0 & 0.48 & 0.96 \end{pmatrix} \begin{pmatrix} N_n \\ J_n \\ B_n \end{pmatrix}$$

where  $a$  and  $b$  are constants, and  $N_n$ ,  $J_n$  and  $B_n$  are the respective numbers of the mammals in each category  $n$  months after the start of the study.

At the start of the study the colony has breeders only, with no newborns or juveniles.

According to the model, after 2 months the number of newborns is 48 and the number of juveniles is 40

- (b) (i) Determine the number of mammals in the colony at the start of the study.  
(ii) Show that  $a = 0.8$  (4)
- (c) Determine, in terms of  $b$ ,

$$\begin{pmatrix} 0 & 0 & 2 \\ 0.8 & b & 0 \\ 0 & 0.48 & 0.96 \end{pmatrix}^{-1}$$
(3)

Given that the model predicts approximately 1015 mammals **in total** at the start of a particular month, and approximately 596 **newborns**, 464 **juveniles** and 437 **breeders** at the start of the next month,

- (d) determine the value of  $b$ , giving your answer to 2 decimal places. (3)

It is decided to monitor the number of **newborn** males and females as a part of the study. Assuming that 42% of newborns are male,

- (e) refine the matrix equation for the model to reflect this information, giving a reason for your answer.  
(There is no need to estimate any unknown values for the refined model, but any known values should be made clear.) (2)











